The Use of Snyder Synthetic Hydrograph for Simulation of Overland Flow in Small Ungauged and Gauged Catchments

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Abstract

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The paper presents the results of simulated overland flow on the Třebsín experimental area, Czech Republic, using the Snyder synthetic unit hydrograph. In this research an attempt was made to discover a new approach to overland flow simulation that could give precise results like the KINFIL model for a small ungauged catchment. The provided results also include a comparison with the KINFIL model for N=10, 20, 50 and 100 year recurrence of rainfall-runoff, with the rainfall time duration $t_d=10, 20, 30, 30$, and 60 min. Concerning a small gauged catchment, one of the most accurate and elegant methodologies, Matrix Inversion Model, can be used for the measurement of both the gross rainfall and the runoff. This method belongs to a matrix algebra concept. For the sake of completeness, we designated this model at the end of the present article to show how exact this forward march can be.

Keywords: extreme rainfall; infiltration intensity; KINFIL model; Matrix Inversion Model; Snyder unit hydrograph

One of the main problems in hydrological studies is the prediction of runoff from an ungauged basin, since the majority of small catchments are ungauged (Hrachowitz *et al.* 2013). The data on rainfall events are often available for such basins, however the simulation of runoff is much more complicated than for the basins with well observed data of runoff discharges. In addition, it is even more sophisticated for the small ungauged catchments (Parajka *et al.* 2013). There are many different approaches to the solution of such a hydrological riddle.

In 1932 the unit hydrograph method was introduced by Sherman (1932) and changed the runoff-rainfall modelling forever. It has become the most widely used method of flood analysis for gauged basins. In spite of obvious advantages, simplicity and applicability of this method, it has one big imperfection: it cannot be used on the basins with lack of data. For the extension of the unit hydrograph theory for

ungauged basins the synthesis from physical characteristics should be considered as an effective and necessary measure.

Currently, there exist several methods for developing the synthetic unit hydrograph using measurable physical basin characteristics. As the founder of the unit hydrograph theory, Sherman was the first to study the possibilities of developed method extension. The physical characteristics of the basin he thought to have an impact on the hydrograph and possibly could be used for the estimation of runoff on the ungauged basins are: the shape and size of the drainage area, slopes of valley sides and mainstream, distribution of water channels and ponding due to course or surface obstacles. As the basis of most synthetic unit hydrograph methods researchers still use Sherman's ideas. Major part of the methods try to find relationships between physical basin parameters and unit hydrograph characteristics, the differences

are in the used methodologies or in recognized relationships (Ellouze-Gargouri & Bargaoui 2012; Singh *et al.* 2014; Rigon *et al.* 2016). Those methods for developing a synthetic hydrograph for ungauged areas have been made by Bernard (1935), Snyder (1938), McCarthy (1939) and Clark (1945).

The final step of our study was a Matrix Inversion Model calculation. The basics of this methodology were developed by SNYDER (1961), through the concepts of matrices and vectors. The convolution of excess rainfall with the T-hour Unit Hydrograph (TUH) is simply the process of multiplication of a matrix by a vector.

The present study was conducted in the Třebsín experimental area. The surface runoff simulation was done using two different approaches: Snyder synthetic unit hydrograph method and kinematic wave based on the KINFIL model.

MATERIAL AND METHODS

This paper describes the continuation of research outcomes from the article published by Fedorova *et al.* (2017), using the HEC-HMS SCS Unit Hydrograph and KINFIL model to compute the surface runoff from extreme rainfall in the small ungauged Kninice catchment. One of the articles mentioning the unit hydrograph was published by Černohous and Kovář (2009) due to approximation of the recession limb of the hydrograph. The KINFIL model is currently used for simulating erosion processes and for predicting the vulnerability of soil to water, since the surface runoff and water erosion are closely related. In the calculation, we designed rainfall events on experimental plots No. 4 and 5 in Třebsín, which are located about

40 km from Prague in south-east direction, close to the village of Třebsín. The location of Experimental Runoff Area (ERA) is depicted in Figure 1.

In sum, there are nine experimental plots, the length of each is 36 m and the width is 7 m. The average slope of the experimental area is about 7°. The research location is operated by the Research Institute for Soil and Water Conservation in Prague-Zbraslav (RISWC Prague). The area belongs to a mildly warm region, with annual mean precipitation of 517 mm, average temperature of 6.5°C and an altitude of 340–350 m a.s.l. The natural soil composition is originally a gneiss substrate and is mostly of Haplic Cambisol type, belonging to the soil group of silty loam.

The scheme of experimental runoff plots is presented in Figure 2. The studied plots are highlighted in green colour.

Rainfall data. The rainfall data from the Benešov station was used for runoff simulation in the Třebsín catchment. This rain gauge provides daily rainfall data with a return period N=2, 5, 10, 50 and 100 years. Due to the small catchment area, the selected periods of critical rainfall time duration are $t_d=20$, 30 and 60 min and the return period of N=10, 20, 50 and 100 years. To compute the reduction in the daily rainfall depths $P_{t,N}$ the DES_RAIN procedure (http://fzp.czu.cz/vyzkum) was used (Vaššová & Kovář 2011). The procedure is based on regional parameters a and c, derived by the methodology of Hrádek and Kovář (1994). The results are provided in Table 1.

Field measurements. The average values for saturated hydraulic conductivity K_s (mm/min) and for sorptivity S (mm/min^{0.5}) were obtained by the infiltrometer method (double cylinders).

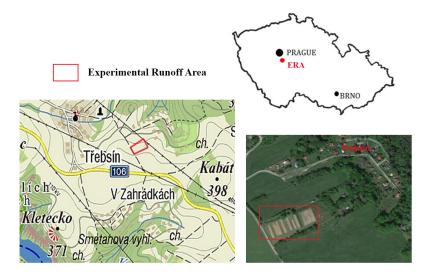


Figure 1. The location of the Experimental Runoff Area (ERA)

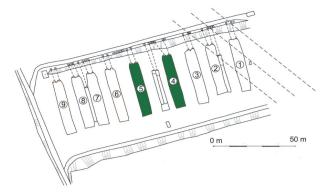


Figure 2. The scheme of runoff plots

Richards' equation (Kutílek & Nielsen 1994) combined with Philip's solution for non-steady flow infiltration (Philip 1957) was implemented for the calculation of hydraulic soil parameters. Simplified Philip's equation for infiltration intensity v_f calculated with saturated hydraulic conductivity $K_{\rm s}$ (m/s) and sorptivity S (m/s^{0.5}) is as follows:

$$v_f(t) = \frac{1}{2} S \times t^{-1/2} + K_s \tag{1}$$

Subsequently, parameters K_s and S were both computed, applying the non-linear regression method (Kovář $et\,al.$ 2011; Štibinger 2011). Table 2 provides the measured hydraulic conductivity K_s , sorptivity S, and the storage suction factor S_f (mm):

$$S_f = \frac{S^2}{2K_s} \tag{2}$$

Snyder Unit Hydrograph. The unit hydrograph is a universal solution for any basin rainfall-runoff relationship providing the single storm hydrograph parameters given the excess rainfall data. However, a major part of watersheds has no recorded rainfall or runoff data. The answer is in the synthesis of unit

Table 1. Maximum rainfall depths $P_{t,N}$ at the Benešov station (mm)

N	$P_{t,N}$ (mm)	t (min)				
(years)		10	20	30	60	
2	38.6	12.8	15.7	17.7	20.5	
5	52.9	18.6	23.0	26.1	31.4	
10	62.0	22.3	28.3	32.6	38.9	
20	71.6	27.2	34.7	40.1	48.1	
50	83.3	33.4	42.9	49.7	60.3	
100	92.4	37.9	49.2	57.2	69.3	

hydrographs – estimating the simple rainfall-runoff relationship by application of physical parameters of drainage basin.

In 1938, a concept of the synthetic unit hydrograph was introduced by Snyder. The methodology is based on the detailed and structured analysis of a large number of hydrographs from different catchments in the Appalachian region. The study led to the following formula (3) for time lag (PONCE 1989):

$$T_{lag} = C_t \left(L L_c \right)^{0.2} \tag{3}$$

where:

 T_{lag} – catchment time lag (h)

 C_t – coefficient explaining the catchment gradient and related to catchment storage

L – mainstream length (km)

 L_c — mainstream length from outlet to the closest point to the catchment centroid (km)

Snyder's formula for peak discharge is as follows (Ponce 1989):

$$Q_p = \frac{2.78 \times C_p \times A}{T_{lag}} \tag{4}$$

where

 Q_p – peak discharge related to 1 cm of effective rainfall (m³/s)

A – catchment area (km²)

 C_p – empirical coefficient connected with triangular base time to time lag

KINFIL rainfall-runoff model. The KINFIL model is used for simulation of significant rainfall-runoff events or for estimation of design discharge in catchments that are impacted by human activities. The kinematic wave techniques are generally considered to be sufficient for the analysis of overland and channel flow. This method is a simplified version of the dynamic wave theory.

The current version of presented model consists of two parts. The first part is based on the Green-Ampt infiltration theory with ponding time according to Mein and Larson (1973) and Morel-Seytoux

Table 2. The soil hydraulic parameters: saturated hydraulic conductivity (K_s), sorptivity (S), and storage suction factor (S_t)

Plot	$S \text{ (mm/min}^{0.5})$	K_s (mm/min)	S_f (mm)
4	4.64	4.36	2.47
5	4.13	1.65	5.17

(Morel-Seytoux & Verdin 1981; Morel-Seytoux

$$K_{s}\left(z_{f} + H_{f} / z_{f}\right) = \left(\theta_{s} - \theta_{i}\right) dz_{f} / dt \tag{5}$$

$$S_f = (\theta_s - \theta_i) \times H_f \tag{6}$$

$$t_p = S_f / i \times \left(\frac{i}{K_s} - 1\right) \tag{7}$$

where:

 K_{c} – hydraulic conductivity (m/s)

 z_f – vertical extent of the saturated zone (m)

 $\dot{\theta}_{c}$ – water content at natural saturation (–)

 θ_i – initial water content (–)

 H_f – wetting front suction (m)

i – rainfall intensity (m/s)

 S_f – storage suction factor (m)

 t_p - ponding time (s) t - time (s)

In small experimental catchments the hydraulic conductivity K_s and the storage suction factor S_f can be measured directly.

The overland flow part of the model uses the kinematic equation and can be described by Eq. (8) (Kibler & Woolhiser 1970; Beven 2006):

$$\frac{\partial y}{\partial t} + \alpha \times m \times y^{m-1} \times \frac{\partial y}{\partial x} = r_e(t)$$
 (8)

where:

 $r_a(t)$ – rainfall excess intensity (m/s)

y, t, x – ordinates of the depth of water, time and position (m, s, m)

α, m - hydraulic parameters

Matrix Inversion Model. One of the most accurate mathematical models for known rainfall and runoff parameters is the Matrix Inversion Model. The basic processes of this method have been developed in the Tennessee Valley Authority (TVA) study by SNYDER (1961). The detailed view if the process involved in the convolution of discrete values of TUH with the rainfall excess to produce the direct runoff through summation is provided by Equation 9 (O'DONNELL

$$Q_{m+n-1} = \Delta T \times \sum_{1}^{m+n-1} P_m \times U_{m-n}$$
 (9)

where:

 $Q - \text{runoff} (m^3/s)$

P – rainfall (mm/h)

U – unit hydrograph ordinates

m – number of rainfall intervals

n – number of isochrone areas (equals to the number of TUH ordinates)

 ΔT – length of time period (h)

When $\Delta T \rightarrow 0$, then the summation can be replaced by Duhamel's convolution integral:

$$Q(t) = \int_{0}^{t} P(\tau) \times U(t - \tau) d\tau$$
 (10)

where:

Q(t) – direct runoff (m³/s)

dummy time variable (-)

Eq. (9) shows that basically the process is the multiplication of a matrix by a vector. However, this means to solve m + n - 1 equations of n unknown values of TUH. Consequently, it is an overdetermined system of m-1 equations and it can hardly be solved by the substitution method. This computation suits the matrix algebra very well (Figure 3):

The matrix equivalent of the equations of Figure 3 is given by Figure 4:

The matrix technique suggested in the abovementioned TVA study (SNYDER 1961) automatically provides a least-squares solution to TUH ordinates. Precipitation *P* should be replaced by the letter *X* (only for rainfall, e.g. liquid form of precipitation);

$$\begin{split} Q_1 &= P_1 * U_1 &+ 0 &+ 0 \ldots \ldots \ldots \ldots \ldots + 0 &+ 0 \\ Q_2 &= P_2 * U_1 + P_1 * U_2 + 0 \ldots + 0 \ldots \ldots \ldots \ldots \ldots + 0 &+ 0 \\ Q_3 &= P_3 * U_1 + P_2 * U_2 + P_1 * U_3 &+ 0 \ldots + 0 \ldots \ldots + 0 &+ 0 \\ Q_m &= P_m * U_1 + P_{m-1} * U_2 + P_{m-2} * U_3 &+ \cdots + P_1 * U_m &+ 0 \\ Q_{m+1} &= 0 &+ P_m * U_2 + P_2 * U_m &+ \cdots \ldots + P_1 * U_{m+1} &+ 0 \\ Q_{m+n-1} &= 0 &+ 0 &+ 0 &+ 0 &+ \cdots \ldots + P_m * U_n \end{split}$$

Figure 3. The group of equations relating rainfall and unit hydrograph ordinates to runoff

Figure 4. Matrix equivalent of discrete convolution equations

Q by the letter *Y* for discharge and the usual notation, the matrix equation can be written:

$$|X| \times |U| = |Y| \tag{11}$$

To solve Eq. (11) for |U|, one must first make the rectangular matrix |X| a square one. This can be done by multiplying both sides of Eq. (11) by the transpose of $|X|^T$ left side, which is the matrix created by interchanging the rows and the columns of |X| in Equation 12:

$$|X|^T \times |X| \times |U| = |Z| \times |U| = |X|^T \times |Y|$$
 (12)

where:

$$|X|^T \times |X| = |Z| \tag{13}$$

$$|A| = |X|^T \times |Y| \tag{14}$$

$$|U| = |Z|^{-1} \times |X|^{T} \times |Y| = |Z|^{-1} \times |A|$$
(15)

The computed vector |U| gives the procedure finding the TUH ordinates directly from a gross rainfall step by step to reach a net rainfall up to a direct runoff |YC| (Y computed) using standard matrix routines:

$$|YC| = |X| \times |U| \tag{16}$$

Hidden in the manipulation of the matrix algebra on the right side of Eq. (16) is the least-squares curve fitting technique mentioned above but to repeat it to requested close coincidence with a net rainfall and T-Unit Hydrograph ordinates. The improved rainfall data is now used to find a better estimate of the TUH and the whole process is repeated.

We were testing the Matrix Inversion Model on a dangerous event in the Jilovsky River catchment. The flooding occurred on 4-5 of July in 2009 (24 h) when a gross rain was falling for about 10 hours. The difference in gross and net rainfall was extremely large: 80-10.25=69.75 (mm). Table 3 provides the basic parameters of the Jilovsky catchment.

RESULTS AND DISCUSSION

The Unit Hydrograph (UH) was first proposed by SHERMAN (1932), originally named unit-graph.

Table 3. Jilovsky catchment parameters

Catchment area (km²)	45.6	Land use (%)	
Elevation (m a.s.l.)	730-249	Forest	52.8
Length of river (km)	11.1	Grassland	37.0
River slope (%)	10.3	Urban areas	9.4
Slope of catchment (%)	14.2	Water areas	0.8

The UH is a very simple and effective method of the rainfall-runoff simulation, however it cannot be used if there is a lack of data. In this case the synthetic unit hydrograph modifications should be used (Clark's, Snyder's, SCS). Since the majority of small watersheds have no recorded runoff or rainfall data, it must be a synthetic hydrograph.

SNYDER (1938) presented a method of deriving synthetic unit graphs empirically. The study and analysis of rainfall-runoff characteristics were done in ungauged and gauged catchments of the Appalachian Mountains of the Eastern United States. There are two main parameters for the Snyder synthetic UH: the lag factor (C_t) and the peak flow factor (C_p) . These parameters are topographically dependent and should be estimated for each particular case. In this study both those parameters were derived from measured data (Melching & Marquardt 1997; Ramírez 2000). Snyder's method was chosen for this study also because it is a part of HEC-HMS software.

Many researches have studied the implementation of the Snyder hydrograph, since it is one of the most popular solutions for the ungauged catchments. In their research Hoffmeister and Weisman (1977) used the synthetic unit hydrograph for an ungauged basin in New Zealand. The authors simulated the runoff using three different methods: Snyder's method, SCS dimensionless hydrograph and Commons' dimensionless method in six basins of two hydrological regions. The synthetic UH were compared with unit hydrographs based on observed data. The results of research show that Snyder's method is reasonably accurate.

In Europe a good representative study of synthetic unit hydrographs was conducted in Poland, in the Grabinka catchment by Wałęga *et al.* (2011). The research results show that both Clark's and Snyder's methods are applicable, with slightly better results of Snyder's method. The publication also contains an interesting approach to the estimation of necessary parameters for simulation.

The previous study on a comparison of SCS synthetic unit hydrograph and KINFIL model showed that KINFIL model provided better results due to the more natural form of hydrograph. The comparison of simulated runoff by KINFIL model and Snyder's method shows that the Snyder synthetic hydrograph improved results compared to a previous study on the SCS synthetic unit hydrograph.

Figure 5 demonstrates the results of simulation for plots 4 and 5 of the Třebsín ERA. The simulation by

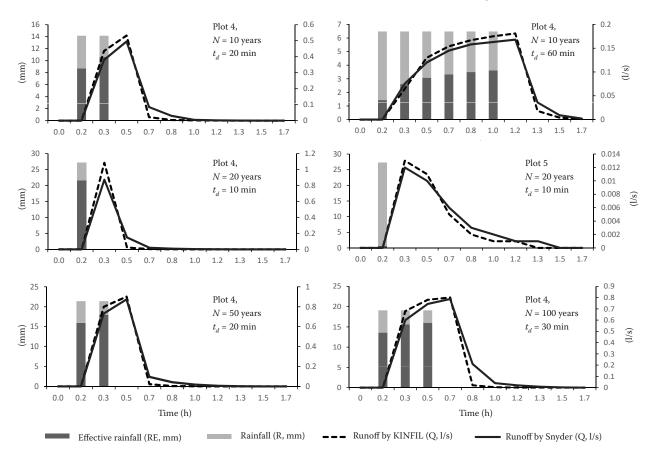


Figure 5. The comparison of hydrographs simulated by KINFIL model and Snyder synthetic unit hydrograph, Třebsín Experimental Runoff Area; N – recurrence interval; t_d – time duration

both models was made on rainfall with recurrence interval $N=10,\,20,\,50,\,100$ years, time duration $t_d=10,\,20,\,30,\,{\rm and}\,60$ min.

The Matrix Inversion method was well described by Dooge and O'Kane (2003) and by Mays (2010). If the unit hydrograph is described, it can be used to

determine a direct runoff for any storm event by the Matrix Inversion method. Because of the simplicity and accuracy of this method it is quite popular in different variations and climatic conditions among hydrology engineers. The study on the Johor River in Malaysia was done by RAZI *et al.* (2010). The syn-

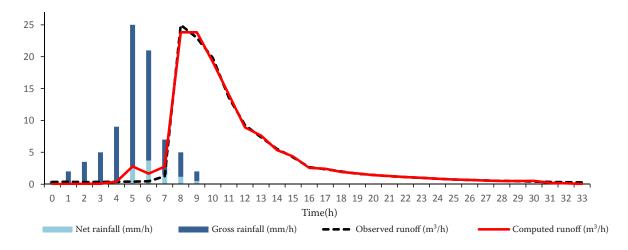


Figure 6. The hydrograph computed by Matrix Inversion method

thetic flood hydrographs were calculated using the SCS Unit Hydrograph method and the convolution matrix procedure.

The results of the Matrix Inversion Model for the Jilovsky catchment are presented in Table 4. The calculated hydrograph is presented in Figure 6.

The successfulness of calibration and validation of models is usually described by the Nash and Sut-

Table 4. The matrix hydrograph reconstruction

Time	Gross rainfall	Net rainfall	Observed runoff	Computed runoff	Unit-
(h)	(mn	n/h)	(m	graph	
0	0.5	0	0.35	0	0.104
1	2	0.01	0.36	0.01	0.267
2	3.5	0.05	0.33	0.04	0.316
3	5	0.15	0.35	0.06	0.332
4	9	0.49	0.37	0.39	0.141
5	25	2.73	0.4	2.78	0.090
6	21	3.7	0.45	1.66	0.007
7	7	1.5	1.23	2.75	0.093
8	5	1.14	24.97	23.82	0.026
9	2	0.48	22.98	23.83	0.055
10	0	0	19.79	19.16	0.006
11	0	0	13.56	14.03	0.022
12	0	0	9.25	8.9	0.013
13	0	0	7.37	7.63	0.018
14	0	0	5.53	5.34	0.007
15	0	0	4.21	4.35	0.010
16	0	0	2.66	2.56	0.008
17	0	0	2.34	2.42	0.007
18	0	0	1.98	1.92	0.005
19	0	0	1.64	1.68	0.006
20	0	0	1.44	1.41	0.003
21	0	0	1.25	1.27	0.006
22	0	0	1.12	1.1	0
23	0	0	0.98	0.99	0.009
24	0	0	0.85	0.84	0
25	0	0	0.73	0.74	0
26	0	0	0.65	0.65	0
27	0	0	0.59	0.57	0
28	0	0	0.52	0.5	0
29	0	0	0.46	0.5	0
30	0	0	0.4	0.52	0
31	0	0	0.35	0.2	0
32	0	0	0.31	0.13	0
33	0	0	0.27	0.05	0

cliffe Coefficient of Efficiency (CE). In the case of the maximum coincidence CE = 1.00. The equation for the Nash and Sutcliffe coefficient calculation is:

$$CE = 1 - \frac{\sum_{i=1}^{n} (Q_i - Q_c)^2}{\sum_{i=1}^{n} (Q_i - \bar{Q})^2}$$
(17)

where:

 Q_i – observed runoff (m³/s)

 Q_c – computed runoff (m³/s)

 \overline{Q} – mean value of observed runoff (m³/s)

n – number of runoff ordinates

Coefficient of efficiency for the current study is CE = 0.989, which is considered to be very high. The efficiency of the Jilovsky catchment is surprisingly accurate.

CONCLUSION

Among all available models for runoff simulation in ungauged catchments different variations of the synthetic unit hydrograph take the leading place, however, it was necessary to consider that there are many effective, physically based models. The previous study showed that the main disadvantage of the applied SCS synthetic unit hydrograph method was its less natural shape. Snyder's method of the synthetic hydrograph is obviously free of this disadvantage. Nonetheless, the main difficulty is the derivation of necessary coefficients. If this problem can be solved in any manner, this method is considered to be effective for runoff simulation in ungauged catchments, yet, it needs further research on catchments under different conditions. Hydrology as a science expands quickly and a new developed technology shows the priority of physically based methods in gauged catchments. New methodology, such as various time series (Fourier series, Laguerre function, etc.) and inversion via matrices, is developed rapidly in terms of mathematical modelling.

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